

Solution

TRIANGLES

Class 10 - Mathematics

Section A

1.

(b) 5

Explanation:

In $\triangle ADE$ and $\triangle ABC$

angle A common

angle D=B angle ($DE \parallel BC$ then, d = b)

by AA similarity criteria

$\triangle ADE$ similar $\triangle ABC$.

$$\frac{AD}{DB} = \frac{DE}{BC}$$

$$\frac{2}{3} = \frac{DE}{7.5}$$

$$DE = 5 \text{ cm.}$$

2.

(c) $\frac{6}{7}$

Explanation:

Given: $\triangle ABC \sim \triangle PQR$

Therefore,

$$\frac{\text{Perimeter of } \triangle ABC}{\text{Perimeter of } \triangle PQR} = \frac{AB}{PQ}$$

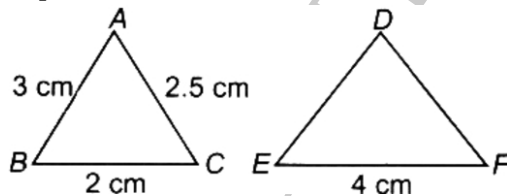
$$= \frac{56}{48} = \frac{AB}{PQ}$$

$$\Rightarrow \frac{PQ}{AB} = \frac{6}{7}$$

3.

(d) 15 cm

Explanation:



Since, $\triangle DEF \sim \triangle ABC$ [Given]

$$\Rightarrow \frac{AB}{DE} = \frac{BC}{EF} \Rightarrow \frac{3}{DE} = \frac{2}{4} \Rightarrow DE = 6 \text{ cm}$$

$$\text{Also, } \frac{AC}{DF} = \frac{BC}{EF} \Rightarrow \frac{2.5}{DF} = \frac{2}{4} \Rightarrow DF = 5 \text{ cm}$$

\therefore Perimeter of $\triangle DEF = DE + EF + FD$

$$= 6 \text{ cm} + 4 \text{ cm} + 5 \text{ cm} = 15 \text{ cm}$$

4.

(b) Statements (ii) is correct.

Explanation:

If a line is drawn parallel to one side of the triangle to intersect the other two sides in distinct points, then the other two sides are divided in the same ratio.

5.

(d) $\angle B = \angle P$

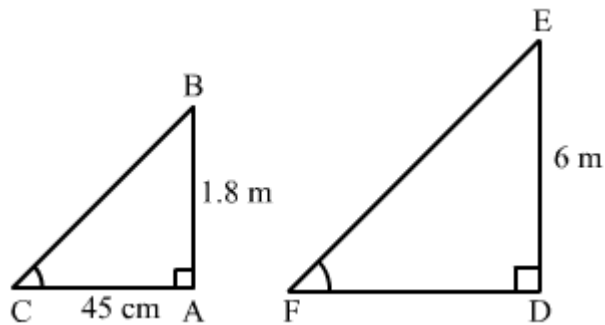
Explanation:

$$\angle B = \angle P$$

6.

(c) 1.5 m

Explanation:



Let AB and AC be the vertical stick and its shadow, respectively.

According to the question:

$$AB = 1.8 \text{ m}$$

$$AC = 45 \text{ cm} = 0.45 \text{ m}$$

Again, let DE and DF be the pole and its shadow, respectively.

According to the question:

$$DE = 6 \text{ m}$$

$$DF = ?$$

Now, in right-angled triangles ABC and DEF, we have:

$$\angle BAC = \angle EDF = 90^\circ$$

$$\angle ACB = \angle DFE \text{ (Angular elevation of the Sun at the same time)}$$

Therefore, by AA similarity theorem,

we get: $\triangle ABC \sim \triangle DEF$

$$\Rightarrow \frac{AB}{AC} = \frac{DE}{DF} \Rightarrow \frac{1.8}{0.45} = \frac{6}{DF} \Rightarrow DF = \frac{6 \times 0.45}{1.8} = 1.5 \text{ m}$$

7.

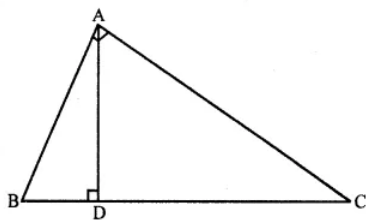
(d) $\left(\frac{AB}{AC}\right)^2$

Explanation:

In right angled $\triangle ABC$, $\angle A = 90^\circ$

$AD \perp BC$

$\therefore \triangle ABD \sim \triangle ABC$



$$\frac{AB}{BC} = \frac{BD}{AB} \Rightarrow AB^2 = BD \times BC \text{(i)}$$

Similarly $\triangle ACD \sim \triangle ABC$

$$DC \times BC = AC^2 \text{(ii)}$$

Dividing (ii) by (i)

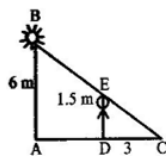
$$\frac{BD \times BC}{DC \times BC} = \frac{AB^2}{AC^2} \Rightarrow \frac{BD}{DC} = \frac{AB^2}{AC^2}$$

$$\text{Hence } \frac{BD}{DC} = \frac{AB^2}{AC^2}$$

8.

(b) 9 m

Explanation:



In triangles ABC and DEC,

$$\angle A = \angle D \text{ [Each } 90^\circ]$$

$$\angle C = \angle C \text{ [Common]}$$

Therefore, $\triangle ABC \sim \triangle DEC$ [AA similarity]

$$\Rightarrow \frac{AB}{DE} = \frac{AC}{DC}$$

$$\Rightarrow \frac{6}{1.5} = \frac{AC}{3}$$

$$\Rightarrow AC = 12 \text{ m}$$

Therefore, the distance between the woman and pole is $12 - 3 = 9 \text{ m}$

9.

(b) 5.4 cm.

Explanation:

Given: $\triangle PQR \sim \triangle XYZ$

$$\therefore \frac{\text{Perimeter of } \triangle PQR}{\text{Perimeter of } \triangle XYZ} = \frac{QR}{YZ}$$

$$\Rightarrow \frac{30}{18} = \frac{9}{YZ}$$

$$\Rightarrow YZ = 5.4 \text{ cm}$$

10.

(b) 2 cm

Explanation:

In $\triangle ABP$ and $\triangle CDP$

$$\angle A = \angle C \text{ (given)}$$

$$\angle APB = \angle CPD \text{ (Vert. oppo. angle)}$$

$\therefore \triangle ABP \sim \triangle CDP$ (by AA criteria)

$$\frac{AB}{CD} = \frac{AP}{CP}$$

$$CD = \frac{AB \times CP}{AP}$$

$$= \frac{6 \times 4}{12} = 2 \text{ cm}$$

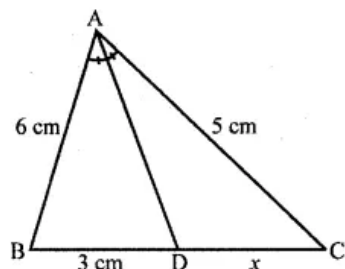
11.

(d) 2.5 cm

Explanation:

In $\triangle ABC$, AD is the bisector of $\angle BAC$

AB = 6 cm, AC = 5 cm, BD = 3 cm



Let $DC = x$

In $\triangle ABC$

\therefore AD is the bisector of $\angle A$

$$\therefore \frac{AB}{AC} = \frac{BD}{DC} \Rightarrow \frac{6}{5} = \frac{3}{x}$$

$$\Rightarrow x = \frac{3 \times 5}{6} = \frac{5}{2} = 2.5$$

$\therefore DC = 2.5 \text{ cm}$

12. (a) 80°

Explanation:

Given:

$$\therefore \triangle ABC \sim \triangle DEF,$$

$$\angle A = \angle D \text{ (by CPST)}$$

$$\angle B = \angle E \text{ (by CPST)}$$

$$\angle C = \angle F \text{ (by CPST)}$$

And, In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + \angle E + \angle C = 180^\circ$$

$$55 + 45 + \angle C = 180$$

$$100 + \angle C = 180$$

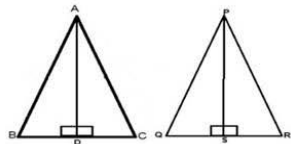
$$\angle C = 180 - 100$$

$$= 80^\circ$$

13.

(c) 35 cm

Explanation:



Given: $\triangle ABC \sim \triangle PQR$

$$\therefore \frac{\text{Perimeter of } \triangle ABC}{\text{Perimeter of } \triangle PQR} = \frac{AB}{PQ}$$

$$\Rightarrow \frac{\text{Perimeter of } \triangle ABC}{25} = \frac{9.1}{6.5}$$

$$\Rightarrow \text{Perimeter of } \triangle ABC = 35 \text{ cm}$$

14. (a) $\angle B = \angle D$

Explanation:

We know that,

By the **SAS similarity criterion**, if one angle of a triangle is equal to one angle of another triangle and the sides including these angles are in the same ratio, then the triangles are similar.

Since the angle formed by AB and BC is $\angle B$.

And, the angle formed by DE and DF is $\angle D$.

So, $\angle B = \angle D$ By [SAS similarity criterion]

Therefore, the given triangles will be similar when $\angle B = \angle D$.

15.

(d) 5.4 cm

Explanation:

$$\triangle ABC \sim \triangle DEF$$

$$\therefore \frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF}$$

$$= \frac{AB+BC+AC}{DE+EF+DF} = \frac{30}{18}$$

$$BC = 9 \text{ cm}$$

$$\therefore \frac{9}{EF} = \frac{30}{18} \Rightarrow EF = \frac{9 \times 18}{30} = \frac{27}{5}$$

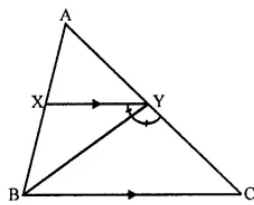
$$\therefore EF = 5.4 \text{ cm}$$

16. (a) $BC = CY$

Explanation:

In $\triangle ABC$, $XY \parallel BC$

Also BY is the bisector $\angle XYC$



$$\angle XYB = \angle CYB \dots\dots (i)$$

$$XY \parallel BC$$

$$\angle XYB = \angle YBC \text{ (Alternate angles are equal) } \dots\dots (ii)$$

$$\angle CYB = \angle YBC$$

$$BC = CY$$

17.

(b) (i) 8.75 m, (ii) 12 m

Explanation:

i. Since, $CD \parallel AB$ [Given]

\therefore In $\triangle RCD$ and $\triangle RBA$, we have

$$\angle BAR = \angle RDC \text{ [Alternate interior angles]}$$

$$\angle ABR = \angle RCD$$

$\therefore \triangle RCD \sim \triangle RBA$ [By AA similarity]

$$\Rightarrow \frac{RB}{RC} = \frac{AB}{DC}$$

$$\Rightarrow \frac{7.5}{1.2} = \frac{AB}{1.4} \Rightarrow AB = \frac{7.5 \times 1.4}{1.2} = 8.75 \text{ m}$$

i.e., Distance between the parks through town is 8.75 m.

ii. In right $\triangle CRD$, we have

$$(CD)^2 = (CR)^2 + (RD)^2$$

$$\Rightarrow RD^2 = (1.4)^2 - (1.2)^2 = 0.52 \Rightarrow RD = 0.72 \text{ m}$$

Since, $\triangle RCD \sim \triangle RBA$

$$\therefore \frac{RB}{RC} = \frac{AR}{DR} \Rightarrow \frac{7.5}{1.2} = \frac{AR}{0.72}$$

$$\Rightarrow AR = \frac{7.5 \times 0.72}{1.2} = 4.5 \text{ m}$$

i.e., Distance from Park A to Park B through point R = $AR + RB = 4.5 \text{ m} + 7.5 \text{ m} = 12 \text{ m}$

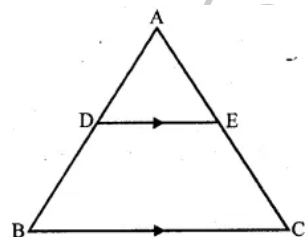
18.

(d) 4.4 cm

Explanation:

In $\triangle ABC$, $DE \parallel BC$

$$AD : DB = 3 : 1, EA = 3.3 \text{ cm}$$



Let $EC = x$

\therefore In $\triangle ABC$, $DE \parallel BC$

$$\frac{AD}{DB} = \frac{AE}{EC} \Rightarrow \frac{3}{1} = \frac{3.3}{x}$$

$$\Rightarrow x = \frac{3.3}{3} = 1.1 \text{ cm}$$

$$\therefore AC = AE + EC = 3.3 + 1.1 = 4.4 \text{ cm}$$

19.

20.

(d) A is false but R is true.

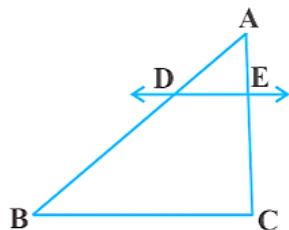
Explanation:

Similar triangles are not always congruent.

21. (a) Both A and R are true and R is the correct explanation of A.

Explanation:

We know that if a line is parallel to one side of a triangle then it divides the other two sides in the same ratio. This is the Basic Proportionality theorem. So, the Reason is correct.



By Basic Proportionality theorem, we have $\frac{AD}{DB} = \frac{AE}{EC}$

$$\Rightarrow \frac{DB}{AD} = \frac{EC}{AE} \Rightarrow \frac{DB}{AD} + 1 = \frac{EC}{AE} + 1$$

$$\Rightarrow \frac{DB+AD}{AD} = \frac{EC+AE}{AE} \Rightarrow \frac{AB}{AD} = \frac{AC}{AE} \Rightarrow \frac{AD}{AB} = \frac{AE}{AC}$$

So, the Assertion is correct.

22.

- (c) A is true but R is false.

Explanation:

A is true but R is false.

23.

- (d) A is false but R is true.

Explanation:

We have,

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\frac{7x-4}{3x+4} = \frac{5x-2}{3x}$$

$$21x^2 - 12x = 15x^2 + 20x - 6x - 8$$

$$6x^2 - 26x + 8 = 0$$

$$3x^2 - 13x + 4 = 0$$

$$3x^2 - 12x - x + 4 = 0$$

$$3x(x-4) - 1(x-4) = 0$$

$$(x-4)(3x-1) = 0$$

$$x = 4, \frac{1}{3}$$

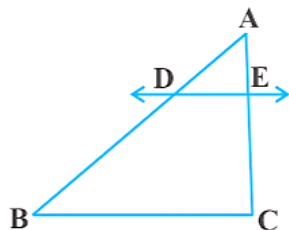
So, A is false but R is true.

24.

- (b) Both A and R are true but R is not the correct explanation of A.

Explanation:

We know that if a line is parallel to one side of a triangle then it divides the other two sides in the same ratio. This is the Basic Proportionality theorem.



So, Reason is correct.

$$DB = 10.8 - 6.3 = 4.5 \text{ cm and } AE = 9.6 - 4 = 5.6 \text{ cm}$$

$$\text{Now, } \frac{AD}{DB} = \frac{6.3}{4.5} = \frac{63}{45} = \frac{7}{5} \text{ and } \frac{AE}{EC} = \frac{5.6}{4} = \frac{56}{40} = \frac{7}{5}$$

$$\Rightarrow \frac{AD}{DB} = \frac{AE}{EC}$$

By Converse of Basic Proportionality theorem, $DE \parallel BC$

So, Assertion is correct.

But reason (R) is not the correct explanation of assertion (A).

25.

(b) Both A and R are true but R is not the correct explanation of A.

Explanation:

Two similar triangles of equal area are always congruent.

26.

(d) A is false but R is true.

Explanation:

If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side. This is the Converse of the Basic Proportionality theorem.

So, the Reason is correct.

$$\text{Now, } \frac{AD}{DB} = \frac{5.7}{9.5} = \frac{57}{95} = \frac{3}{5}$$

$$\text{and } \frac{AE}{EC} = \frac{4.8}{8} = \frac{48}{80} = \frac{3}{5}$$

$$\Rightarrow \frac{AD}{DB} = \frac{AE}{EC}$$

By Converse of Basic Proportionality theorem, $DE \parallel BC$

So, the Assertion is not correct.

27.

(c) A is true but R is false.

Explanation:

A is true but R is false.

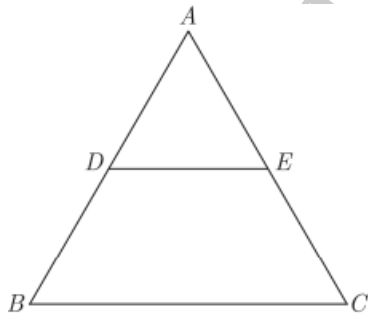
28. (a) Both A and R are true and R is the correct explanation of A.

Explanation:

Reason is true: [This is Thale's Theorem]

For Assertion

Since, $DE \parallel BC$ by Thale's Theorem



$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\frac{DB}{AD} = \frac{EC}{AE}$$

$$1 + \frac{DB}{AD} = 1 + \frac{EC}{AE}$$

$$\frac{AD+DB}{AD} = \frac{AE+EC}{AE}$$

$$\frac{AB}{AD} = \frac{AC}{AE}$$

Assertion is true.

Since, reason gives Assertion.

29.

(b) Both A and R are true but R is not the correct explanation of A.

Explanation:

If a line divides any two sides of a triangle in the same ratio then it is parallel to the third side. This is the Converse of the Basic Proportionality theorem.

So, the Reason is correct.

By Basic Proportionality theorem, we have $\frac{AD}{DB} = \frac{AE}{EC} \Rightarrow \frac{4}{x-4} = \frac{8}{3x-19}$

$$\Rightarrow 4(3x - 19) = 8(x - 4)$$

$$\Rightarrow 12x - 76 = 8x - 32$$

$$\Rightarrow 4x = 44 \Rightarrow x = 11 \text{ cm}$$

So, Assertion is correct.

But reason (R) is not the correct explanation of assertion (A).

Section B

30. 30

Explanation:

In the given figure, EF || BD and CE is the transversal.

$\therefore \angle CAD = \angle AEF$ (Pair of corresponding angles)

$$\Rightarrow \angle CAD = 55^\circ$$

In $\triangle ABC$

$\angle CAD = \angle ABC + \angle ACB$ (Exterior angle of a triangle is equal to the sum of the two interior opposite angles)

$$\Rightarrow 55^\circ = \angle ABC + 25^\circ$$

$$\Rightarrow \angle ABC = 55^\circ - 25^\circ = 30^\circ$$

Thus, the measure of $\angle ABC$ is 30°

31. 16

Explanation:

According to question it is given that triangles ABC and PQR are similar.

Also, perimeter of $\triangle ABC = 32$ & Perimeter of $\triangle PQR = 24$

Therefore,

$$\frac{\text{Perimeter}(\triangle ABC)}{\text{Perimeter}(\triangle PQR)} = \frac{AB}{PQ}$$

$$\Rightarrow \frac{32}{24} = \frac{AB}{12}$$

$$\Rightarrow AB = \frac{32 \times 12}{24}$$

$$= 16 \text{ cm}$$

32. 4

Explanation:

According to question it is given that ABC is a triangle in which DE || BC.

Also, AD = 8 cm, AB = 15 cm, EC = 3.5 cm

Applying Thales' theorem, we get:

$$\frac{AD}{AB} = \frac{AE}{AC}$$

$$\Rightarrow \frac{8}{15} = \frac{AE}{AE+EC}$$

$$\Rightarrow \frac{8}{15} = \frac{AE}{AE+3.5}$$

$$\Rightarrow 8AE + 28 = 15AE$$

$$\Rightarrow 7AE = 28$$

$$\Rightarrow AE = 4 \text{ cm}$$

33. 1.5

Explanation:

Given XY || BC

AX = 1 cm, XB = 3 cm, and BC = 6 cm

$$AB = AX + XB$$

$$= 1 + 3 = 4 \text{ cm}$$

In $\triangle AXY$ and $\triangle ABC$

$$\angle A = \angle A \text{ [Common]}$$

$$\angle AXY = \angle ABC \text{ [Corresponding angles]}$$

Then, $\triangle AXY \sim \triangle ABC$ [By AA similarity]

$$\therefore \frac{AX}{AB} = \frac{XY}{BC} \text{ [Corresponding parts of similar } \triangle \text{ are proportional]}$$

$$\Rightarrow \frac{1}{4} = \frac{XY}{6}$$

$$\Rightarrow XY = \frac{6}{4} = 1.5\text{cm}$$

34. 18

Explanation:

According to question It is given that in $\triangle ABC$, AE is the bisector of the $\angle CAD$.

Also, $BE = BC + CE = 12 + x$

$CE = x$, $AB = 10$, $AC = 6$

Since, We know that, the external bisector of an angle of a triangle divides the opposite side internally in the ratio of the sides containing the angle.

$$\therefore \frac{BE}{CE} = \frac{AB}{AC}$$

$$\Rightarrow \frac{12+x}{x} = \frac{10}{6}$$

$$\Rightarrow 6(12+x) = 10x$$

$$\Rightarrow 72 + 6x = 10x$$

$$\Rightarrow 4x = 72$$

$$\Rightarrow x = \frac{72}{4}$$

$$= 18\text{ cm}$$

$$\Rightarrow CE = 18\text{ cm}$$

35. 1.5

Explanation:

According to question it is given that

$DE \parallel BC$, $AB = 6\text{ cm}$ and $AE = \frac{1}{4}AC$

In $\triangle ADE$ and $\triangle ABC$

$\angle A = \angle A$ [Common]

$\angle ADE = \angle ABC$ [Corresponding angles]

Then, $\triangle ADE \sim \triangle ABC$ [By AA similarity]

$\Rightarrow \frac{AD}{AB} = \frac{AE}{AC}$ [because in similar triangles Corresponding parts of similar \triangle are proportional]

$$\Rightarrow \frac{AD}{6} = \frac{\frac{1}{4}AC}{AC} \left[\because AE = \frac{1}{4}AC \text{ given} \right]$$

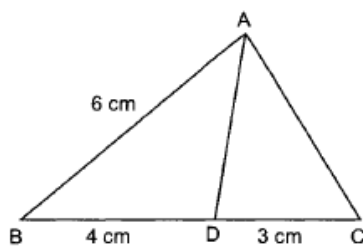
$$\Rightarrow \frac{AD}{6} = \frac{1}{4}$$

$$\Rightarrow AD = \frac{6}{4} = 1.5\text{cm}$$

36. 4.5

Explanation:

In $\triangle ABC$, AD is the bisector of $\angle A$.



According to question it is given that

$BD = 4\text{ cm}$, $CD = 3\text{ cm}$ and $AB = 6\text{ cm}$

We know that, the bisector of an angle of a triangle divides the opposite side internally in the ratio of the sides containing the angle.

$$\therefore \frac{BD}{DC} = \frac{AB}{AC}$$

$$\Rightarrow \frac{4}{3} = \frac{6}{AC}$$

$$\Rightarrow 4 AC = 18$$

$$\Rightarrow AC = \frac{9}{2}\text{ cm} = 4.5\text{cm} .$$

37. According to question it is given that triangles ABC and PQR are similar.

Also, perimeter of $\triangle ABC = 32$ & Perimeter of $\triangle PQR = 24$

Therefore,

$$\frac{\text{Perimeter } (\triangle ABC)}{\text{Perimeter } (\triangle PQR)} = \frac{AB}{PQ}$$

$$\Rightarrow \frac{32}{24} = \frac{AB}{12}$$

$$\Rightarrow AB = \frac{32 \times 12}{24}$$

$$= 16 \text{ cm}$$

38. According to question,

it is given that In $\triangle ABC$, $LM \parallel CB$

Therefore, by Thales' theorem

$$\Rightarrow \frac{AM}{AB} = \frac{AL}{AC} \dots(i)$$

In $\triangle ACD$, $LN \parallel CD$

Therefore by Thales theorem

$$\Rightarrow \frac{AL}{AC} = \frac{AN}{AD} \dots\dots\dots(ii)$$

From (i) and (ii) we get

$$\frac{AM}{AB} = \frac{AN}{AD}$$

39. We have,

$$\frac{AD}{DB} = \frac{2}{3} \text{ and } DE \parallel BC$$

Therefore, by basic proportionality theorem, we have,

$$\frac{AD}{DB} = \frac{AE}{EC}$$

Taking reciprocal on both sides, we get

$$\frac{DB}{AD} = \frac{EC}{AE}$$

$$\Rightarrow \frac{3}{2} = \frac{EC}{AE}$$

Adding 1 on both sides, we get

$$\frac{3}{2} + 1 = \frac{EC}{AE} + 1$$

$$\Rightarrow \frac{3+2}{2} = \frac{EC+AE}{AE}$$

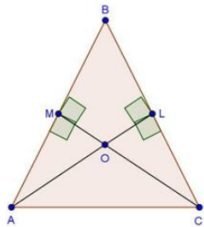
$$\Rightarrow \frac{5}{2} = \frac{AC}{AE} \quad [\because AE + EC = AC]$$

$$\Rightarrow \frac{5}{2} = \frac{18}{AE} \quad [\because AC = 18]$$

$$\Rightarrow AE = \frac{18 \times 2}{5}$$

$$\Rightarrow AE = \frac{36}{5} = 7.2 \text{ cm}$$

40. We have,



We are given that,

$AL \perp BC$ and $CM \perp AB$

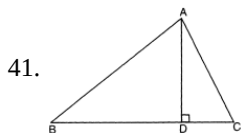
i. In $\triangle OMA$ and $\triangle OLC$

$\angle MOA = \angle LOC$ [Vertically opposite angles]

$\angle AMO = \angle CLO$ [Each 90°]

ii. Then, $\triangle OMA \sim \triangle OLC$ [By AA similarity]

$\therefore \frac{OA}{OC} = \frac{OM}{OL}$ [Corresponding parts of similar \triangle are proportional]



41.

$$AD^2 = BD \times CD$$

$$\text{or, } \frac{AD}{CD} = \frac{BD}{AD}$$

Therefore, $\triangle ADC \sim \triangle BDA$ (by SAS)

or, $\angle BAD = \angle ACD$;

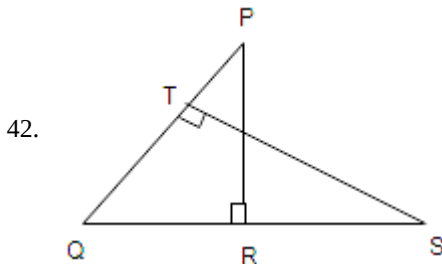
$\angle DAC = \angle DBA$ (Corresponding angles of similar triangles)

$\angle BAD + \angle ACD + \angle DAC + \angle DBA = 180^\circ$ [sum of angles of \triangle]

or, $2\angle BAD + 2\angle DAC = 180^\circ$

or, $\angle BAD + \angle DAC = 90^\circ$

Therefore, $\angle A = 90^\circ$



In $\triangle PRQ$ and $\triangle STQ$,

$\angle PRQ = \angle STQ$ [\because Each 90°]

$\angle PQR = \angle SQT$ [\because common angle]

So, $\triangle PRQ \sim \triangle STQ$ [By AA similarity criterion]

$$\Rightarrow \frac{QR}{QT} = \frac{QP}{QS}$$

[since, corresponding sides of similar triangles are proportional]

$$\Rightarrow QR \times QS = QP \times QT$$

Hence proved.

43. In $\triangle ABC$ and $\triangle AMP$

$\angle ABC = \angle AMP$... (i) [Each equal to 90°]

$\angle BAC = \angle MAP$... (ii) [Common angle]

$\triangle ABC \sim \triangle AMP$ (AA similarity criterion)

44. We have

$PQ = 1.28$ cm, $PR = 2.56$ cm, $PE = 0.18$ cm, $PF = 0.36$ cm

$EQ = PQ - PE = 1.28 - 0.18 = 1.10$ cm

and $FR = PR - PF = 2.56 - 0.36 = 2.20$ cm

Now we can find

$$\frac{PE}{EQ} = \frac{0.18}{1.10} = \frac{9}{55}$$

$$\frac{PF}{FR} = \frac{0.36}{2.20} = \frac{9}{55}$$

$$\therefore \frac{PE}{EQ} = \frac{PF}{FR}$$

$\therefore EF \parallel QR$ (By converse of basic proportionality theorem)

45. We have

$$\frac{DE}{QR} = \frac{2.5}{5} = \frac{1}{2}$$

$$\frac{EF}{PQ} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{DF}{PR} = \frac{3}{6} = \frac{1}{2}$$

$$\Rightarrow \frac{DE}{QR} = \frac{EF}{PQ} = \frac{DF}{PR}$$

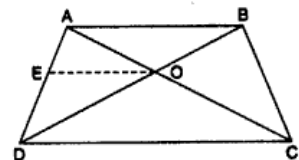
Therefore, by SSS similarity theorem, $\triangle FED \sim \triangle PQR$.

46. Given: The diagonals of a quadrilateral ABCD intersect each other at the point O such that $\frac{AO}{BO} = \frac{CO}{DO}$

To prove: ABCD is trapezium.

Construction: Through O draw a line $OE \parallel BA$ intersecting AD at E.

Proof: In $\triangle DBA$: $\because OE \parallel BA$



$$\therefore \frac{DO}{BO} = \frac{DE}{AE} \Rightarrow \frac{CO}{AO} = \frac{DE}{AE}$$

$$\therefore \frac{AO}{BO} = \frac{CO}{DO} \text{ [Given]}$$

$$\Rightarrow \frac{DO}{BO} = \frac{CO}{AO} \Rightarrow \frac{AO}{CO} = \frac{AE}{DE} \text{[Taking reciprocals]}$$

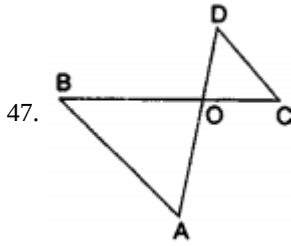
\therefore In $\triangle ADC$

$OE \parallel CD$ [By converse basic proportionality theorem]

But $OE \parallel BA$

BA || CD.....[By construction]
The quadrilateral ABCD is a Trapezium.

Section C



i. Let OA be x cm

Since it is given that $\triangle OAB \sim \triangle OCD$

Therefore, $\frac{OA}{OC} = \frac{AB}{CD}$

$$\Rightarrow \frac{x}{3.5} = \frac{8}{5}$$

$$\Rightarrow x = \frac{8 \times 3.5}{5}$$

$$= 5.6$$

Hence, OA = 5.6 cm.

ii. Let OD be Y cm

Since it is given that $\triangle OAB \sim \triangle OCD$

$$\therefore \frac{AB}{CD} = \frac{OB}{OD}$$

$$\Rightarrow \frac{8}{5} = \frac{6.4}{y}$$

$$\Rightarrow y = \frac{6.4 \times 5}{8}$$

$$= 4$$

Hence, DO = 4 cm

48. It is given $DE \parallel BC$

Applying Thales' theorem, we get:

$$\frac{AD}{BD} = \frac{AE}{EC}$$

$$\Rightarrow \frac{7x-4}{3x+4} = \frac{5x-2}{3x}$$

$$\Rightarrow 3x(7x-4) = (5x-2)(3x+4)$$

$$\Rightarrow 21x^2 - 12x = 15x^2 + 20x^2 - 6x - 8$$

$$\Rightarrow 21x^2 - 12x = 15x^2 + 14x - 8$$

$$\Rightarrow 6x^2 - 26x + 8 = 0$$

$$\Rightarrow 2(3x^2 - 13x + 4) = 0$$

$$\Rightarrow 3x^2 - 13x + 4 = 0$$

$$\Rightarrow 3x^2 - 12x - x + 4 = 0$$

$$\Rightarrow 3x^2(x-4) - 1(x-4) = 0$$

$$\Rightarrow (x-4)(3x-1) = 0$$

$$\Rightarrow x-4 = 0 \text{ or } 3x-1 = 0$$

$$\Rightarrow x-4 \text{ or } x = \frac{1}{3}$$

If $x = \frac{1}{3}$, $7x-4 = -\frac{5}{3} < 0$; It is not possible.

Therefore, $x = 4$

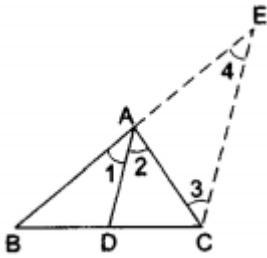
49. In $\triangle RPQ$ and $\triangle RTS$,

$\angle R = \angle R$ (common)

$\angle P = \angle RTS$ (given)

$\Rightarrow \triangle RPQ \sim \triangle RTS$ (AA similarity)

50.



It is given that in $\triangle ABC$, D is a point on BC such that $\frac{BD}{DC} = \frac{AB}{AC}$.

To Prove: AD is the bisector of $\angle A$.

Construction: Produce BA to E such that AE = AC and Join EC.

Proof: $\frac{BD}{DC} = \frac{AB}{AC}$ (given)

$\Rightarrow \frac{BD}{DC} = \frac{AB}{AE}$ [$\because AC = AE$]

$\Rightarrow DA \parallel CE$ [by the converse of Thales' theorem]

$\therefore \angle 2 = \angle 3$ (i) [alternate interior angle]

and $\angle 1 = \angle 4$ (ii) [corresponding angle]

Also, AE = AC

$\Rightarrow \angle 3 = \angle 4$ (iii)

$\therefore \angle 1 = \angle 2$ [from (i), (ii) and (iii)].

Hence, AD is the bisector of $\angle A$.

51. Given: Right triangles $\triangle ABC$ and $\triangle DBC$ are drawn on the same hypotenuse BC on the same side of BC.

Also, AC and BD intersect at P.

We have to show: $AP \times PC = BP \times PD$

Now, In $\triangle BAP$ and $\triangle CDP$, we have

$\angle BAP = \angle CDP = 90^\circ$

$\angle BPA = \angle CPD$ (vertically opposite angles)

$\therefore \triangle BAP \sim \triangle CDP$ [by AA-similarity]

$\therefore \frac{AP}{DP} = \frac{BP}{CP}$

$\Rightarrow AP \times CP = BP \times DP$

$\Rightarrow AP \times PC = BP \times PD$

Hence, $AP \times PC = BP \times PD$.

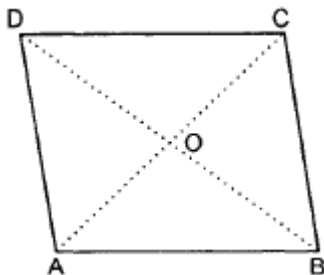
52. **GIVEN** A quadrilateral ABCD in which the diagonal BD bisects $\angle B$ and $\angle D$.

TO PROVE $\frac{AB}{BC} = \frac{AD}{CD}$

CONSTRUCTION Join AC intersecting BD in O.

PROOF We know that the internal bisector of an angle of a triangle divides the opposite side internally in the ratio of the sides containing the angle.

In $\triangle ABC$, BO is the bisector of $\angle B$.



$\therefore \frac{AO}{OC} = \frac{BA}{BC}$

$\Rightarrow \frac{OA}{OC} = \frac{AB}{BC}$ (1)

In $\triangle ADC$, DO is the bisector of $\angle D$.

$\therefore \frac{AO}{OC} = \frac{DA}{DC}$

$\Rightarrow \frac{OA}{OC} = \frac{AD}{CD}$ (2)

From (1) and (2), we get $\frac{AB}{BC} = \frac{AD}{CD}$

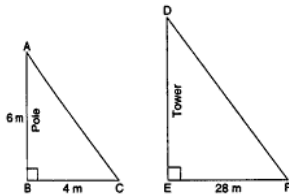
53. Let AB denoted the vertical pole of length 6m. BC is the shadow of the pole on the ground BC = 4m.

Let DE denote the tower.

EF is shadow of the tower on the ground.

EF = 28 m.

Let the height of the tower be h m.



In $\triangle ABC$ and $\triangle DEF$,

$\angle B = \angle E$ [Each equal to 90° because pole and tower are standing vertical to the ground]

$\angle C = \angle F$ [Same elevation]

$\angle A = \angle D$ \therefore shadows are cast at the same time

$\therefore \triangle ABC$ and $\triangle DEF$,

$\angle B = \angle E$ [Each equal to 90° because pole and tower are standing vertical to the ground.]

$\angle A = \angle D$ (\therefore shadows are cast at the same time)

$\therefore \triangle ABC \sim \triangle DEF$ (AA similarity criterion)

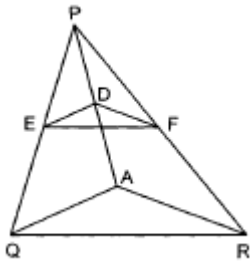
$\therefore \frac{AB}{DE} = \frac{BC}{EF}$ [\therefore corresponding sides of two similar triangles are proportional]

$$\Rightarrow \frac{6}{h} = \frac{4}{28}$$

$$\Rightarrow h = \frac{6 \times 28}{4} \Rightarrow h = 42$$

Hence, the height of the tower is 42 m

54.



$DE \parallel AQ$ [Given]

Therefore, by basic proportionality theorem, we have

$$\frac{PE}{EQ} = \frac{PD}{DA} \text{(1)}$$

In $\triangle PAR$, we have

$DF \parallel AR$ [Given]

Therefore, by basic proportionality theorem, we have

$$\frac{PD}{DA} = \frac{PF}{FR} \text{(2)}$$

From (1) and (2), we have

$$\frac{PE}{EQ} = \frac{PF}{FR}$$

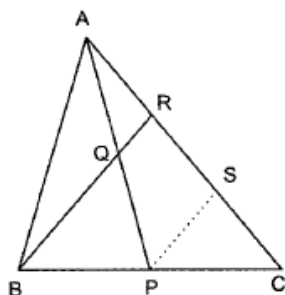
$\Rightarrow EF \parallel QR$ [By the converse of Basic Proportionality Theorem]

55. **GIVEN:** A $\triangle ABC$ in which P is the mid-point of BC, Q is the mid-point of BR and, Q is also the mid-point of AP such that BQ produced meets AC at R.

TO PROVE $RA = \frac{1}{3}CA$.

CONSTRUCTION: Draw $PS \parallel BR$, meeting AC at S.

PROOF: In $\triangle BCR$, P is the mid-point of BC and $PS \parallel BR$.



\therefore S is the mid-point of CR.

$$\Rightarrow CS = SR \dots(i)$$

In $\triangle APS$, Q is the mid-point of AP and $QR \parallel PS$.

\therefore R is the mid-point of AS.

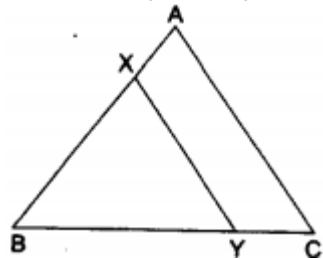
$$\Rightarrow AR = RS \dots(ii)$$

From (i) and (ii), we get

$$AR = RS = SC$$

$$\Rightarrow AC = AR + RS + SC = 3 AR$$

$$\Rightarrow AR = \frac{1}{3} AC = \frac{1}{3} CA$$



56.

Since $XY \parallel AC$, we have

$\angle A = \angle BXY$ and $\angle C = \angle BYX$ (corresponding angles)

$\therefore \triangle ABC \sim \triangle XBY$

$$\Rightarrow \frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle XBY)} = \frac{AB^2}{XB^2} \dots\dots\dots(i)$$

But, $\text{ar}(\triangle ABC) = 2 \times \text{ar}(\triangle XBY)$ [Given]

$$\Rightarrow \frac{\text{ar}(\triangle ABC)}{\text{ar}(\triangle XBY)} = 2 \dots\dots\dots(ii)$$

From (i) and (ii), we have

$$\frac{AB^2}{XB^2} = 2$$

$$\Rightarrow \left(\frac{AB}{XB}\right)^2 = 2$$

$$\Rightarrow \frac{AB}{XB} = \sqrt{2}$$

$$\Rightarrow AB = \sqrt{2}(XB)$$

$$\Rightarrow AB = \sqrt{2}(AB - AX)$$

$$\Rightarrow \sqrt{2}AX = (\sqrt{2} - 1)AB$$

$$\Rightarrow \frac{AX}{AB} = \frac{(\sqrt{2}-1)}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = \frac{(2-\sqrt{2})}{2}$$

$$\text{or } AX : AB = (2 - \sqrt{2}) : 2 .$$

Section D

57. i. Figures A and C are similar.

ii. Only Figure C is congruent.

iii. All congruent figures are similar but all similar figures are not congruent.

For example, a pair of triangles that are similar by the A.A.A. test of similarity are not congruent pairs of triangles since the exact lengths of the sides are unknown.

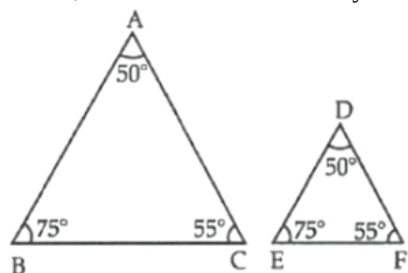
In $\triangle ABC$ and $\triangle DEF$,

$$\angle A = \angle D = 50^\circ,$$

$$\angle B = \angle E = 75^\circ$$

$$\text{and } \angle C = \angle F = 55^\circ.$$

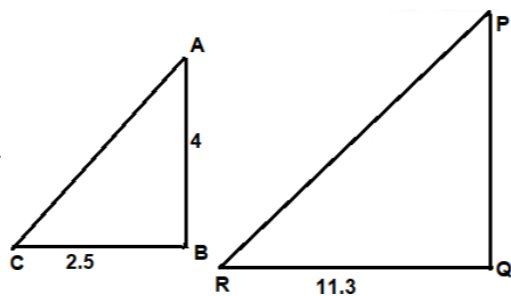
Hence, $\triangle ABC \sim \triangle DEF$ but they are not congruent.



OR

The length of corresponding sides must be equal.

58. i.



Let AB be a wall and PQ is a tree

BC and QR are their shadow respectively at 3 p.m.

$$\therefore \triangle ABC \sim \triangle PQR$$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR}$$

$$\frac{4}{PQ} = \frac{2.5}{11.3}$$

$$2.5 \times PQ = 4 \times 11.3$$

$$PQ = 18.08$$

$$\therefore \text{height of tree} = 18.08 \text{ feet}$$

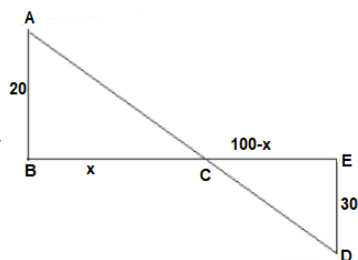
ii. 0

iii. Right triangle

OR

Zero

59. i.



$$\triangle ABC \sim \triangle DEC$$

$$\frac{20}{30} = \frac{x}{100-x}$$

$$2000 - 20x = 30x$$

$$2000 = 50x$$

$$x = 40 \text{ m}$$

ii. AA

iii. 60 metres

OR

$$AD = AC + CD$$

$$= \sqrt{20^2 + 40^2} + \sqrt{60^2 + 30^2}$$

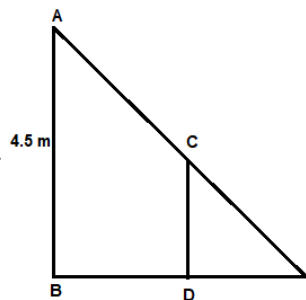
$$= \sqrt{400 + 1600} + \sqrt{3600 + 900}$$

$$= \sqrt{2000} + \sqrt{4500}$$

$$\Rightarrow 20\sqrt{5} + 30\sqrt{5}$$

$$\Rightarrow 50\sqrt{5} \text{ m}$$

60. i.



Distance covered in 2 sec = 2 m

length of shadow = 1 m

Total distance from base = 2 + 1 = 3m

$$\frac{1}{3} = \frac{\text{height of Rohan}}{4.5}$$

height of Rohan = 1.5 m

= 150 cm

ii. When $x > 1.5$ m

distance walked = d m

$$\Rightarrow \frac{x}{d+x} = \frac{1.5}{4.5}$$

$$\Rightarrow \frac{x}{d+x} = \frac{1}{3}$$

$$2x = d$$

$$d > 3$$

hence, the time must be 3 sec

\therefore minimum time after which his shadow become larger than his original height = 3 s

iii. 3 metres

OR

After 4 and distance = 4 m

Shadow length = y m

$$\frac{y}{4+y} = \frac{1.5}{4.5}$$

$$3y = 4 + y$$

$$y = 2 \text{ m}$$

\therefore After 4 sec, the shadow length will be 2 m

61. i. $\tan 30^\circ = \frac{1}{\sqrt{3}} = \frac{75}{AB}$

$$\Rightarrow AB = 75\sqrt{3} \text{ cm}$$

ii. $\sin 30^\circ = \frac{1}{2} = \frac{75}{OB}$

$$\Rightarrow OB = 150 \text{ cm}$$

iii. $QB = 150 - 75 = 75 \text{ cm}$

$\Rightarrow Q$ is mid point of OB

Since $PQ \parallel AO$ therefore P is mid pint of AB

$$\text{Hence } AP = \frac{75\sqrt{3}}{2} \text{ cm.}$$

OR

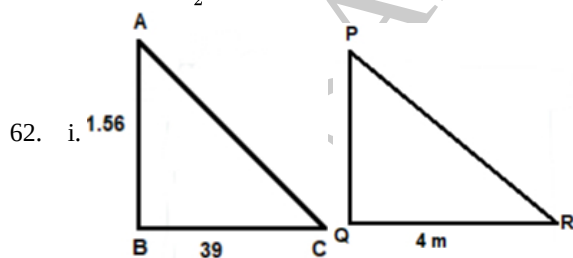
$$QB = 150 - 75 = 75 \text{ cm}$$

Now, $\triangle BQP \sim \triangle BOA$

$$\Rightarrow \frac{QB}{OB} = \frac{PQ}{OA}$$

$$\Rightarrow \frac{1}{2} = \frac{PQ}{75}$$

$$\Rightarrow PQ = \frac{75}{2} \text{ cm}$$



$$\triangle ABC \sim \triangle PQR$$

$$\frac{1.56}{0.39} = \frac{PQ}{4}$$

$$\frac{1.56 \times 4}{0.39} = PQ$$

$$PQ = 16 \text{ m}$$

\therefore height of Pine apple = 16 m.

ii. Height of Kavita = 1.56 m

iii. Right triangle

OR

AA criteria

63. i. Since $\angle D = \angle C$ and $\angle B = \angle A$ (Alternate interior angles)

$\therefore \triangle OAC \sim \triangle OBD$ (By AA similarity)

ii. $\triangle OAC \sim \triangle OBD \Rightarrow \frac{OA}{OB} = \frac{AC}{BD} \text{ or } \frac{OA}{AC} = \frac{OB}{BD}$

$$\text{iii. a. } \triangle OAC \sim \triangle OBD \Rightarrow \frac{OA}{OB} = \frac{OC}{OD}$$

$$\Rightarrow \frac{3x+4}{x} = \frac{3x+19}{x+3} \Rightarrow x = 2$$

$$\therefore OC = 25$$

OR

$$\text{b. } \triangle OBD \sim \triangle OAC \Rightarrow \frac{OB}{OA} = \frac{OD}{OC} = \frac{BD}{AC}$$

$$\Rightarrow \frac{x}{3x+4} = \frac{x+3}{3x+19} \Rightarrow x = 2$$

$$\therefore \frac{BD}{AC} = \frac{2}{10} \text{ or } \frac{1}{5}$$

64. i. Isosceles Triangle

ii. Let $2x$ be the width of window, then $3x$ will be height of window because ratio is $2 : 3$ now width of single curtain will be x because it is half of the window.

Length of single curtain is equal to height of the window.

$$\therefore \text{Ratio} = \frac{x}{3x} = 1 : 3$$

$$\text{iii. Area} = 3x \times 2x$$

$$9600 = 6x^2$$

$$x = 40 \text{ cm}$$

$$\text{breadth} = 80 \text{ cm}$$

$$\text{length} = 120 \text{ cm}$$

OR

$$\text{Perimeter} = 2(l + b)$$

$$= 2(120 + 80)$$

$$= 400 \text{ cm}$$

65. i. $\therefore AF = h$ (Given)

$$\therefore AF = AH + HF$$

$$h = AH + \frac{h}{4}$$

$$AH = h - \frac{h}{4}$$

$$AH = \frac{3h}{4}$$

ii. $\therefore AF = h$ (Given)

$$\therefore AG = \frac{2}{3} AF$$

\therefore centroid divide the median in $2 : 1$

$$\text{iii. } AH = \frac{3h}{4}$$

J is centroid of $\triangle ADE$

$$AJ : JH = 2 : 1$$

let $AJ = 2x$ and $JH = x$

$$2x + x = \frac{3h}{4}$$

$$x = \frac{h}{4}$$

$$AJ = 2 \times \frac{h}{4} = \frac{h}{2}$$

$$AG = AJ + GJ$$

$$= \frac{h}{2} + \frac{h}{6}$$

$$= \frac{2h}{3}$$

$$\text{But } AJ = \frac{h}{2} \times \frac{2}{3}$$

$$AJ = \frac{3}{4} AG$$

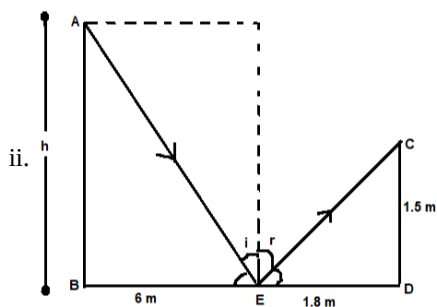
OR

$$GJ = AG - AJ$$

$$= AG - \frac{3}{4} AG$$

$$GJ = \frac{1}{4} AG$$

66. i. AA criterion



$\triangle ABE \sim \triangle CDE$ (by AA criteria)

$$\frac{AB}{CD} = \frac{BE}{DE}$$

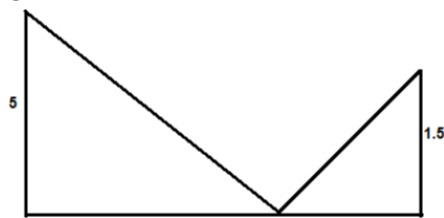
$$h = \frac{6 \times 1.5}{1.8}$$

$$h = 5$$

i.e., height of pole = 5 m.

iii. $\tan i = \frac{6}{5}$

OR



$$\frac{1.5}{5} = \frac{13-x}{x}$$

$$1.5x = 65 - 5x$$

$$6.5x = 65$$

$$x = \frac{65}{6.5}$$

$$= 10$$

\therefore distance of Suresh from mirror

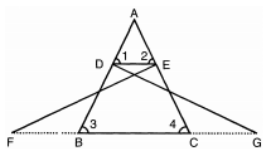
$$= 13 - x$$

$$= 13 - 10$$

$$= 3 \text{ m}$$

Section E

67.



$$\therefore \triangle FEC \cong \triangle GBD$$

$$\text{or, } EC = BD \dots\dots(i)$$

It is given that $\angle 1 = \angle 2$

$$\text{or, } AE = AD \text{ (} \because \text{ Isosceles triangle property) } \dots(ii)$$

From ,eqns. (i) and (ii),

$$\frac{AE}{EC} = \frac{AD}{DB}$$

or, $DE \parallel BC$, (\because converse of B.PT)

or, $\angle 1 = \angle 3$ and $\angle 2 = \angle 4$ (\because Corresponding angles)

Thus in $\triangle ADE$ and $\triangle ABC$,

$$\angle A = \angle A$$

$$\angle 1 = \angle 3$$

$$\angle 2 = \angle 4$$

$$\triangle ADE \sim \triangle ABC \text{ (} \because \text{ AAA criterion of similarity)}$$

$$\triangle ADE \sim \triangle ABC \text{ Hence proved}$$

68. In $\triangle AOF$ and $\triangle BOD$

$$\angle O = \angle O \text{ (Same angle) and } \angle A = \angle B \text{ (each } 90^\circ)$$

Therefore, $\triangle AOF \sim \triangle BOD$ (AA similarity)

$$\text{So, } \frac{OA}{OB} = \frac{FA}{DB}$$

Also, in $\triangle FAC$ and $\triangle EBC$, $\angle A = \angle B$ (Each 90°)

and $\angle FCA = \angle ECB$ (Vertically opposite angles).

Therefore, $\triangle FAC \sim \triangle EBC$ (AA similarity).

$$\text{So, } \frac{FA}{EB} = \frac{AC}{BC}$$

But $EB = DB$ (B is mid-point of DE)

$$\text{So, } \frac{FA}{DB} = \frac{AC}{BC} \quad (2)$$

Therefore, from (1) and (2), we have:

$$\frac{AC}{BC} = \frac{OA}{OB}$$

$$\text{i.e. } \frac{OC - OA}{OB - OC} = \frac{OA}{OB}$$

$$\text{or } OB \cdot OC - OA \cdot OB = OA \cdot OB - OA \cdot OC$$

$$\text{or } OB \cdot OC + OA \cdot OC = 2 OA \cdot OB$$

$$\text{or } (OB + OA) \cdot OC = 2 OA \cdot OB$$

$$\text{or } \frac{1}{OA} + \frac{1}{OB} = \frac{2}{OC} \quad [\text{Dividing both the sides by } OA \cdot OB \cdot OC]$$

69. **Given:** ABCD is a quadrilateral. P, Q, R, and S are the points of trisection of sides AB, BC, CD and DA respectively and are adjacent to A and C.

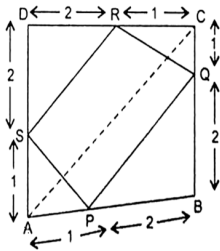
To Prove: PQRS is a parallelogram.

i.e. we have to prove that $PQ \parallel SR$ and $QR \parallel PS$.

Construction: Join AC.

Proof: Since P, Q, R, and S are the points of trisection of AB, BC, CD, and DA respectively.

$$\therefore BP = 2 PA, BQ = 2 QC, DR = 2 RC \text{ and } DS = 2 SA$$



In $\triangle ADC$, we have

$$\frac{DS}{AS} = \frac{2}{1} \text{ and } \frac{DR}{RC} = \frac{2}{1}$$

$$\Rightarrow \frac{DS}{SA} = \frac{DR}{RC}$$

$$\Rightarrow SR \parallel AC \quad \text{----- (i) [by the converse of basic proportionality theorem]}$$

Again,

In $\triangle ABC$, we have

$$\frac{AP}{PB} = \frac{1}{2} \text{ and } \frac{CQ}{QB} = \frac{1}{2}$$

$$\Rightarrow \frac{AP}{AB} = \frac{CQ}{CB}$$

$$\Rightarrow PQ \parallel AC \quad \text{----- (ii) [by the converse of basic proportionality theorem]}$$

From (i) and (ii), we obtain,

$$SR \parallel AC \text{ and } PQ \parallel AC \Rightarrow SR \parallel PQ$$

Similarly, by joining BD, we can prove that $QR \parallel PS$.

Thus, PQRS is a parallelogram.

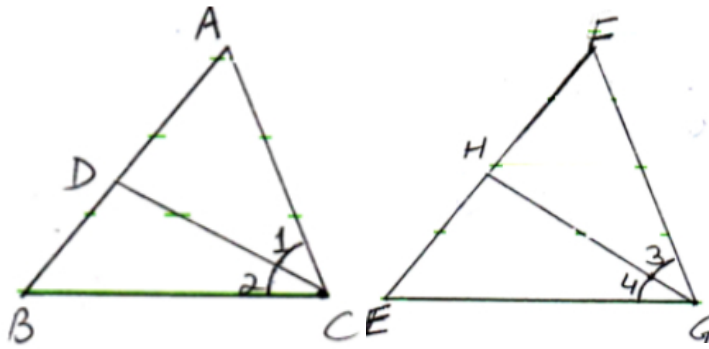
Hence proved.

70. **Given:** $\triangle ABC \sim \triangle FEG$ and CD, GH are bisectors of $\angle ACB$ and $\angle EGF$ respectively.

To Prove

$$\text{i. } \frac{CD}{GH} = \frac{AC}{FG}$$

ii. $\triangle DCB \sim \triangle HGE$



Proof:

i. $\angle ACB = \angle FGE$ ($\triangle ABC \sim \triangle FEG$)

$$\Rightarrow \frac{1}{2} \angle ACB = \frac{1}{2} \angle FGE \text{ (CD and GH are bisectors of } \angle ACB \text{ and } \angle EGF)$$

$$\Rightarrow \angle 1 = \angle 3 \text{ and } \angle 2 = \angle 4$$

In $\triangle ACD$ and $\triangle FGH$

$$\angle A = \angle F (\triangle ABC \sim \triangle FEG)$$

$$\angle 1 = \angle 3 \text{ (proved above)}$$

$$\Rightarrow \triangle ACD \sim \triangle FGH \text{ (AA criteria)}$$

$$\Rightarrow \frac{CD}{GH} = \frac{AC}{FG}$$

ii. In $\triangle DCB$ and $\triangle HGE$

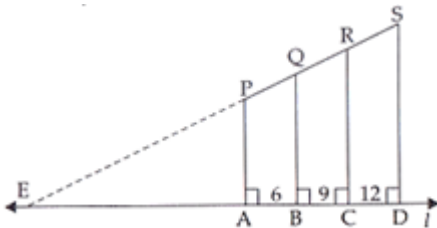
$$\angle B = \angle E (\triangle ABC \sim \triangle FEG)$$

$$\angle 2 = \angle 4 \text{ (proved above)}$$

$$\therefore \triangle DCB \sim \triangle HGE \text{ (AA criteria)}$$

71. **Given:** PA, QB, RC and SD are perpendicular on line l.

$$AB = 6 \text{ cm, } BC = 9 \text{ cm, } CD = 12 \text{ cm, } SP = 36 \text{ cm}$$



To find: PQ, QR and RS.

Construction: we produce SP so that it joins l at E.

Proof: In $\triangle EDS$,

$$AP \parallel BQ \parallel CR \parallel SD \text{ [Given]}$$

$$\therefore PQ : QR : RS = AB : BC : CD$$

$$PQ : QR : RS = 6 : 9 : 12$$

$$\text{Let } PQ = 6x$$

$$\text{then } QR = 9x$$

$$\text{and } RS = 12x$$

$$\text{Now, } PQ + QR + RS = 36 \text{ cm (given)}$$

$$\Rightarrow 6x + 9x + 12x = 36$$

$$\Rightarrow 27x = 36$$

$$\Rightarrow x = \frac{36}{27} = \frac{4}{3}$$

$$\text{Therefore, } PQ = 6 \times \frac{4}{3} = 8 \text{ cm}$$

$$QR = 9 \times \frac{4}{3} = 12 \text{ cm}$$

$$RS = 12 \times \frac{4}{3} = 16 \text{ cm}$$

72. $GF \parallel DE$ (DEFG is square)

$$\therefore \angle AGF = \angle ABC \text{ (Corresponding angles)}$$

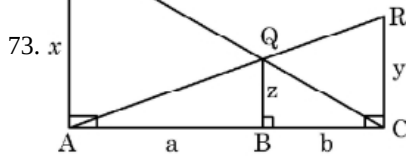
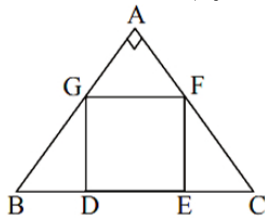
$$\therefore \angle A = \angle GDB = 90^\circ$$

$$\therefore \angle AGF \sim \angle DBG \text{ (By AA similarity)}$$

Again DEFG being a square $\angle AFG = \angle ACB$ (corresponding angles)

$\therefore \angle A = \angle CEF$ (each 90°)

$\angle AGF \sim \angle EFC$ (By AA similarity)



In the given figure we have $PA \perp AC$ and $QB \perp AC$

$\Rightarrow QB \parallel PA$

In $\triangle PAC$ and $\triangle QBC$, we have

$\angle QCB = \angle PCA$ (Common)

$\angle QBC = \angle PAC$ (both are 90°).

So by AA similarity rule, $\triangle QBC \sim \triangle PAC$

$$\therefore \frac{QB}{PA} = \frac{BC}{AC}$$

$$\Rightarrow \frac{z}{x} = \frac{b}{a+b} \dots(i) \text{ [by the property of similar triangles]}$$

In $\triangle RAC$, $QB \parallel RC$.

So, $\triangle QBA \sim \triangle RCA$.

$$\therefore \frac{QB}{RC} = \frac{AB}{AC}$$

$$\Rightarrow \frac{z}{y} = \frac{a}{a+b} \dots(ii) \text{ [by the property of similar triangles]}$$

From (i) and (ii), we obtain

$$\frac{z}{x} + \frac{z}{y} = \left(\frac{b}{a+b} + \frac{a}{a+b} \right) = 1$$

$$\Rightarrow \frac{z}{x} + \frac{z}{y} = 1$$

$$\Rightarrow \frac{1}{x} + \frac{1}{y} = \frac{1}{z}$$

$$\text{or } \frac{1}{x} + \frac{1}{y} = \frac{1}{z}.$$

Hence proved.

74. Given, $AC = 8$ cm, $AD = 3$ cm

and $\angle ADC = \angle BCA$

From the figure in $\triangle ADC$ and $\triangle BCA$

$\angle A = \angle A$...(Common)

$\angle ADC = \angle BCA$...(Given)

So, by AA similarity criteria

$\triangle ADC \sim \triangle BCA$

\therefore Corresponding sides are in the same ratio

$$\frac{AC}{AD} = \frac{AB}{AC}$$

$$\frac{8}{3} = \frac{AB}{8}$$

$$AB = \frac{8 \times 8}{3}$$

$$= \frac{64}{3} \text{ cm}$$

Now from the figure,

$$BD = AB - AD$$

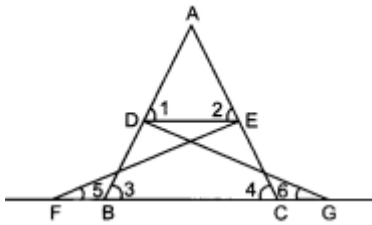
$$= \frac{64}{3} - 3$$

$$= \frac{64-9}{3}$$

$$= \frac{55}{3}$$

$$BD = 18\frac{1}{3} \text{ cm.}$$

75. Given: $\triangle FEC \cong \triangle GBD$ and $\angle 1 = \angle 2$



To prove: $\triangle ADE \sim \triangle ABC$

Proof: In $\triangle ADE$, $\angle 1 = \angle 2$ (Given)

$\Rightarrow AE = AD$ (i) (sides opposite to equal angles are equal)

Also, $\triangle FEC \cong \triangle GBD$ (Given)

$\Rightarrow BD = EC$ (by CPCT)(ii)

$\angle 3 = \angle 4$ [By CPCT]

Also $AE + EC = AD + BD$

$AC = AB$ (iii)

Dividing (i) and (iii), we get

$\frac{AD}{AB} = \frac{AE}{AC}$ and $\angle A = \angle A$ (common)

$\therefore \triangle ADE \sim \triangle ABC$ (SAS similarity)

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