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S.E. (Civil Engg.) (I Sem.) EXAMINATION, 2019 ENGINEERING MATHEMATICS—III

(2015 PATTERN)

Time : Two Hours

Seat

No.

Maximum Marks : 50

- N.B. := (i) Neat diagrams must be drawn wherever necessary.
 - (ii) Assume suitable data, if necessary.
 - (iii) Use of non-programmable calculator is allowed.
 - (iv) Answer Q. Nos. 1 or 2, Q. Nos. 3 or 4, Q. Nos. 5 or
 6, Q. Nos. 7 or 8.

1. (a) Solve any two of the following : [8]
(i)
$$(D^2 - 4D + 4)$$
 $y = e^{2x} \sin 3x$
(ii) $\frac{d^2y}{dx^2} + 4y = \tan 2x$ (by variation of parameters)
(iii) $(x + 1)^2 \frac{d^2y}{dx^2} + (x + 1) \frac{dy}{dx} + y = 2 \sin [\log (x + 1)].$
(b) Solve the following system of equations by Gauss-Jordan method : [4]
 $x_1 + x_2 + x_3 = 9$

 $2x_{1} - 3x_{2} + 4x_{3} = 13$ $3x_{1} + 4x_{2} + 5x_{3} = 40.$

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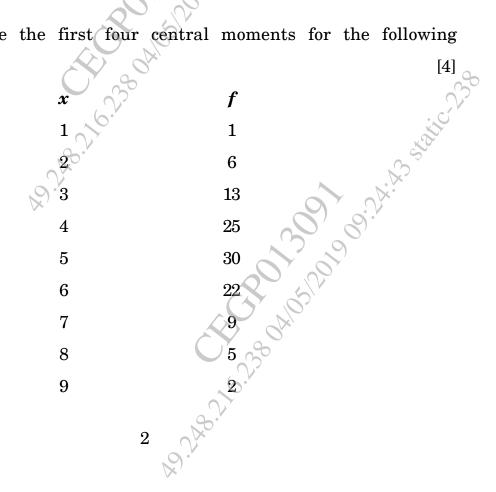
- Orvit Find the elastic curve of a uniform cantilever beam of length 2. (a)l, having a constant weight w kg per foot and determine the deflection of the free end. [4]
 - Using fourth order Runge-Kutta method, solve the equation (*b*) $\frac{dy}{dx} = \sqrt{x + y}$ subject to the conditions x = 0, y = 1 and find y at x = 0.2 taking h = 0.2. [4]
 - Solve the following system of equations by Cholesky's (c)method : [4]

$$4x_1 - 2x_2 = 0$$

$$-2x_1 + 4x_2 - x_3 = 1$$

$$-x_2 + 4x_3 = 0,$$

Calculate the first four central moments for the following 3. (a)data :



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- *(b)* If the probability that an individual suffers a bad reaction from a certain injection is 0.001, determine the probability that out of 2000 individuals, more than 2 individuals will suffer a bad reaction. [4]
- Find the directional derivative of $\phi = 5x^2y 5y^2z + 2z^2x$ at the (c)point (1, 1, 1) in the direction of the line : [4]

$$\frac{x-1}{2} = \frac{y-3}{-2} = \frac{z}{1}.$$
Or
$$Or$$

Prove the following (any one) : 4. [4] $\nabla \cdot \left[r \nabla \left(\frac{1}{r^n} \right) \right] = \frac{n(n-2)}{r^{n+1}}$ (*i*)

For scalar functions ϕ and ψ show that : (ii)

$$\nabla \cdot [\phi \nabla \psi - \psi \nabla \phi] = \phi \nabla^2 \psi - \psi \nabla^2 \phi.$$

- $\overline{\mathbf{F}} = (ye^{xy} \cos z)\overline{i} + (xe^{xy} \cos z)\overline{j} (e^{xy} \sin z)\overline{k}$ that *(b)* Show [4] irrotational. Find ϕ such that $\overline{F} = \nabla \phi$.
- If $\overline{x} = 8.2$, $\overline{y} = 12.4$, $\sigma_x = 6.2$, $\sigma_y = 20$, r(x, y) = 0.9. Find lines of (c)regression. Also estimate the value of x for y = 10 and value

5. Solve any *two* :

of y for x = 10. [4] any two : Using Green's theorem to evaluate $\int_{C} (3y \, dx + 2x \, dy)$, where C (a)is boundary $0 \le x \le \pi$, $0 \le y \le \sin x$. [7]3

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(*b*) Using Divergence theorem to evaluate $\iint_{\mathbf{S}} \left[(2x+3z)i - (xz+y) j + (y^2-2z)k \right] \cdot \overline{d}\mathbf{S}$ where S is the surface of sphere having center at (3, -1,2) and radius is 3. [6] Evaluate $\iint (\nabla \times \overline{F}) \cdot \overline{dS}$ for the surface of paraboloid z = 4(c) $y^2, z \ge 0$ and $\overline{\mathbf{F}} = y^2 i + zj + xyk$. [6] Or 6. Solve any two : Find the workdone in moving a particle along the curve (a) $\overline{r} = a \cos \theta i + a \sin \theta j + b \theta k$ from $\theta = \frac{\pi}{4}$ to $\theta = \frac{\pi}{2}$ under the force field is given by : [7] $\overline{\mathbf{F}} = (-3a\,\sin^2\theta\,.\cos\theta)\,i + a(2\sin\theta - 3\sin^3\theta)j + b\,.\sin\,2\theta k.$ [6] (*b*) Show that : $\int_{\mathbf{C}} [\overline{u} \times (\overline{r} \times \overline{v})] . \overline{d}r = - (\overline{u} \times \overline{v}) . \iint_{\mathbf{S}} d\mathbf{S}$ Where S is the open surface bounded by curve C and $\overline{u}, \overline{v}$ are constant vectors. Using Divergence theorem to show that (c)[6] $\iint_{S} \overline{r} \cdot \overline{n} \ dS = 3V$ where V is the volume enclosed by 'S'.

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- 7. Solve any *two* of the following
 - (a) A tightly stretched string with fixed ends x = 0 and x = l is initially at rest in its equilibrium position. If it is set vibrating giving each point a velocity 3x(l x) for 0 < x < l, find the displacement.
 - *(b)* Solve [6] $\frac{\partial u}{\partial t} = \mathbf{C}^2 \frac{\partial^2 u}{\partial r^2}$ if u is finite for all t(i)u(0, t) = 0 for all t(ii) u(l, t) = 0 for all t(iii) $u(x, 0) = u_0$ for $0 \le x \le 0$. (iv) $\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = 0$ with conditions : Solve the equation *(c)* [6] V = 0 when $y \to \infty$ for all x (i)V(0, y) = 0 for all y (ii)V(1, y) = 0 for all y (iii) V(x, 0) = x(1 - x) for 0 < x < 1. (iv)

Or

8. Solve any two of the following :

(a) A taut string of a length 2l is fastened at both ends. The midpoint of the string is taken to a height b and then released from rest in that position, obtain the displacement. [7]

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temperature 0°C, while over the base temperature of 100°C is maintained. Find steady-state temperature u(x, y). [6]