



JEE Paper 1
ENTRANCE EXAM - JEE MAIN

Time Allowed: 3 hours

Maximum Marks : 300

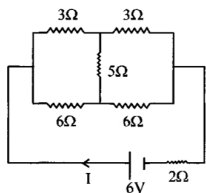
General Instructions:

- All questions are compulsory.
- There are three parts and each part carries 25 questions where the first 20 questions are MCQs and the next 5 questions are numerical.
- You will get 4 marks for each correct response and 1 mark will be deducted for an incorrect answer.

PHYSICS

- 1) The following observations were taken for determining surface tension T of water by the capillary method: Diameter of capillary, $D = 1.25 \times 10^{-2}$ m rise of water, $h = 1.45 \times 10^{-2}$ m Using $g = 9.80$ m/s² and the simplified relation $T = \frac{rhg}{2} \times 10^3$ N/m, the possible error in surface tension is closest to: [4]
- a) 1.5% b) 0.15%
c) 2.4% d) 10%

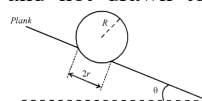
- 2) A battery of 6 V is connected to the circuit as shown below. The current I drawn from the battery is:



[4]

- a) 1A
b) 2 A
c) $\frac{4}{3}$ A
d) $\frac{6}{11}$ A
- 3) A projectile is given an initial velocity of $\hat{i} + 2\hat{j}$. The cartesian equation of its path is: ($g = 10$ m/s²) [4]
a) $Y = 2x - 25x^2$ b) $Y = x - 5x^2$
c) $4y = 2x - 5x^2$ d) $Y = 2x - 5x^2$
- 4) An object flying in air with velocity $(20\hat{i} + 25\hat{j} - 12\hat{k})$ suddenly breaks into two pieces whose masses are in the ratio 1:5. The smaller mass flies off with a velocity $(100\hat{i} + 35\hat{j} + 8\hat{k})$. The velocity of the larger piece will be, [4]
a) $-100\hat{i} - 35\hat{j} - 8\hat{k}$
b) $-20\hat{i} - 15\hat{j} - 80\hat{k}$
c) $4\hat{i} + 23\hat{j} - 16\hat{k}$
d) $20\hat{i} + 15\hat{j} - 80\hat{k}$
- 5) A particle of mass m moving in the x direction with speed $2v$ is hit by another particle of mass $2m$ moving in the same direction with speed v . If the collision is perfectly inelastic, the percentage loss in the energy during the collision is close to: [4]
a) 44% b) 62%
c) 56% d) 50%
- 6) A football of radius R is kept on a hole of radius r ($r < R$) made on a plank kept horizontally. One end of the plank is now lifted so that it gets tilted making an angle θ

from the horizontal as shown in the figure below. The maximum value of θ so that the football does not start rolling down the plank satisfies (the figure is schematic and not drawn to scale)



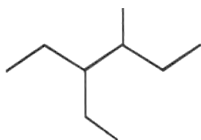
[4]

- a) $\cos\theta = \frac{r}{2R}$
b) $\tan\theta = \frac{r}{R}$
c) $\sin\theta = \frac{r}{2R}$
d) $\sin\theta = \frac{r}{R}$

- 7) Two identical cylindrical vessels are kept on the ground and each contains the same liquid of density d . The area of the base of both vessels is S but the height of liquid in one vessel is x_1 and in the other, x_2 . When both cylinders are connected through a pipe of negligible volume very close to the bottom, the liquid flows from one vessel to the other until it comes to equilibrium at a new height. The change in energy of the system in the process is: [4]
a) $\frac{3}{4}gdS(x_2 - x_1)^2$
b) $gdS(x_2 + x_1)^2$
c) $\frac{1}{4}gdS(x_2 - x_1)^2$
d) $gdS(x_2^2 + x_1^2)$
- 8) An external pressure p is applied on a cube at 0°C so that it is equally compressed from all sides. K is the bulk modulus of the material of the cube and α is its coefficient of linear expansion. Suppose we want to bring the cube to its original size by heating. The temperature should be raised by [4]
a) $\frac{p}{3\alpha K}$ b) $\frac{3\alpha}{pK}$
c) $3pK\alpha$ d) $\frac{p}{\alpha K}$
- 9) A monoatomic gas at pressure P and volume V is suddenly compressed to one eighth of its original volume. The final pressure at constant entropy will be: [4]
a) P b) $32P$
c) $8P$ d) $64P$
- 10) When two displacements represented by $y_1 = a \sin(\omega t)$ and $y_2 = b \cos(\omega t)$ are superimposed the motion is: [4]
a) Simple harmonic with amplitude $\frac{a}{b}$
b) Simple harmonic with amplitude $\sqrt{a^2 + b^2}$
c) Not a simple harmonic
d) Simple harmonic with amplitude $\frac{(a + b)}{2}$
- 11) For the circuit shown in the figure, the charge on $4\mu\text{F}$ capacitor is:

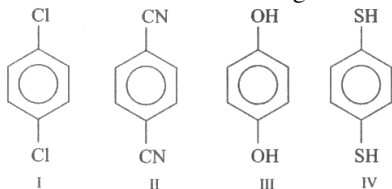
- 28) If K_{sp} of Ag_2CO_3 is 8×10^{-12} , the molar solubility of Ag_2CO_3 in 0.1 M $AgNO_3$ is [4]
- a) 8×10^{-11} M b) 8×10^{-13} M
c) 8×10^{-10} M d) 8×10^{-12} M
- 29) The standard enthalpies of formation of $CO_2(g)$, $H_2O(l)$ and glucose(s) at $25^\circ C$ are - 400 kJ/mol, - 300 kJ/mol and - 1300 kJ/mol, respectively. The standard enthalpy of combustion per gram of glucose at $25^\circ C$ is [4]
- a) +2900 kJ b) +16.11 kJ
c) - 16.11 kJ d) - 2900 kJ
- 30) Which amongst the following is the strongest acid? [4]
- a) $CHCl_3$ b) $CH(CN)_3$
c) CHI_3 d) $CHBr_3$
- 31) Copper becomes green when exposed to moist air for a long period. This is due to: [4]
- a) The formation of a layer of cupric hydroxide on the surface of copper
b) The formation of basic copper sulphate layer on the surface of the metal
c) The formation of a layer of cupric oxide on the surface of copper
d) The formation of a layer of basic carbonate of copper on the surface of copper

- 32) The correct IUPAC name of the following compound is:



[4]

- a) 3, 4 - ethylmethylhexane
b) 3 - ethyl - 4 - methylhexane
c) 4 - ethyl - 3 - methylhexane
d) 4 - methyl - 3 - ethylhexane
- 33) In order to oxidise a mixture of one mole of each of FeC_2O_4 , $Fe(C_2O_4)_3$, $FeSO_4$ and $Fe_2(SO_4)_3$ in acidic medium, the number of moles of $KMnO_4$ required is: [4]
- a) 1 b) 1.5
c) 2 d) 3
- 34) For which of the following molecule significant $\mu \neq 0$?



[4]

- a) I and II b) Only I
c) Only III d) III and IV
- 35) The freezing point of a diluted milk sample is found to be $-0.2^\circ C$, while it should have been $-0.5^\circ C$ for pure milk. How much water has been added to pure milk to make the diluted sample? [4]
- a) 1 cup of water to 2 cups of pure milk
b) 2 cups of water to 3 cups of pure milk
c) 3 cups of water to 2 cups of pure milk
d) 1 cup of water to 3 cups of pure milk

- 36) Evaluate the following statements for their correctness.
- i. The elevation in boiling point temperature of water will be same for 0.1 M NaCl and 0.1 M urea.

- ii. Azeotropic mixtures boil without change in their composition.
iii. Osmosis always takes place from hypertonic to hypotonic solution.
iv. The density of 32% H_2SO_4 solution having molarity 4.09 M is approximately 1.26 gmL^{-1} .
v. A negatively charged sol is obtained when KI solution is added to silver nitrate solution.

[4]

- a) A, B, and D only b) A and C only
c) B and D only d) B, D, and E only

- 37) The decreasing order of electrical conductivity of the following aqueous solutions is:
- i. 0.1 M Formic acid
ii. 0.1 M Acetic acid
iii. 0.1 M Benzoic acid

[4]

- a) $A > B > C$ b) $C > B > A$
c) $C > A > B$ d) $A > C > B$

- 38) NO_2 required for a reaction is produced by the decomposition of N_2O_5 in CCl_4 as per the equation,
 $2N_2O_5(g) \rightarrow 4NO_2(g) + O_2(g)$
The initial concentration of N_2O_5 is 3.00 mol L^{-1} and it is 2.75 mol L^{-1} after 30 minutes. The rate of formation of NO_2 is [4]

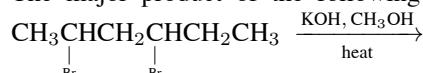
- a) $2.083 \times 10^{-3} \text{ mol L}^{-1} \text{ min}^{-1}$
b) $1.667 \times 10^{-2} \text{ mol L}^{-1} \text{ min}^{-1}$
c) $4.167 \times 10^{-3} \text{ mol L}^{-1} \text{ min}^{-1}$
d) $8.333 \times 10^{-3} \text{ mol L}^{-1} \text{ min}^{-1}$

- 39) The standard electrode potentials ($E_{M^+/M}^\circ$) of four metals A, B, C and D are - 1.2 V, 0.6 V, 0.85 V and - 0.76 V, respectively. The sequence of deposition of metals on applying potential is: [4]
- a) D, A, B, C b) A, C, B, D
c) B, D, C, A d) C, B, D, A

- 40) Aqueous solution of which salt will not contain ions with the electronic configuration $1s^2 2s^2 2p^6 3s^2 3p^6$? [4]
- a) NaF b) KBr
c) NaCl d) CaI_2

- 41) Consider that a d^6 metal ion (M^{2+}) forms a complex with aqua ligands, and the spin - only magnetic moment of the complex is 4.90 BM. The geometry and the crystal field stabilization energy of the complex is: [4]
- a) Tetrahedral and $-0.6\Delta_t$
b) Tetrahedral and $-1.6\Delta_t + 1P$
c) Octahedral and $-1.6\Delta_0$
d) Octahedral and $-2.4\Delta_0 + 2P$

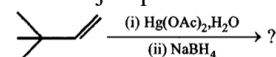
- 42) The major product of the following reaction is:



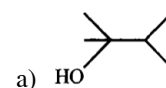
[4]

- a) $CH_3CH=C=CHCH_2CH_3$ b) $CH_2=CHCH=CHCH_2CH_3$
c) $CH_2=CHCH_2CH=CHCH_3$ d) $CH_3CH=CH-CH=CHCH_3$

- 43) The major product in the following reaction

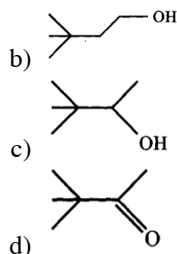


[4]

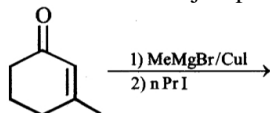


a) HO

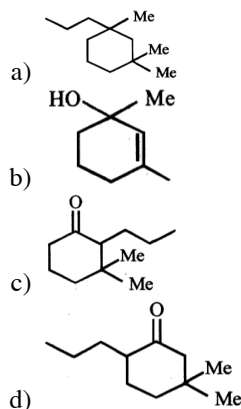
MATHEMATICS



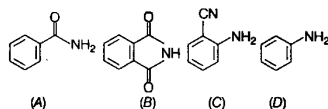
- 44) Find out the major product from the following reaction



[4]



- 45) The increasing order of reactivity of the following compounds towards reaction with alkyl halides directly is



[4]

- a) (B) < (A) < (C) < (D)
 b) (B) < (A) < (D) < (C)
 c) (A) < (B) < (C) < (D)
 d) (A) < (C) < (D) < (B)

- 46) Assume that the radius of the first Bohr orbit of hydrogen atom is 0.6Å . The radius of the third Bohr orbit of He^+ is picometer. (Nearest Integer) [4]

- 47) A first order reaction has the rate constant, $k = 4.6 \times 10^{-3} \text{ s}^{-1}$. The number of correct statement/s from the following is/are _____. Given: $\log 3 = 0.48$

- i. Reaction completes in 1000 s.
 ii. The reaction has a half - life of 500 s.
 iii. The time required for 10% completion is 25 times the time required for 90% completion.
 iv. The degree of dissociation is equal to $(1 - e^{-kt})$.
 v. The rate and the rate constant have the same unit.

[4]

- 48) The total number of unpaired electrons present in the complex $\text{K}_3[\text{Cr}(\text{oxalate})_3]$ is _____. [4]

- 49) A metal surface of 100 cm^2 area has to be coated with nickel layer of thickness 0.001 mm . A current of 2A was passed through a solution of $\text{Ni}(\text{NO}_3)_2$ for x seconds to coat the desired layer. The value of x is _____ (Nearest integer)

(ρ_{Ni} (density of Nickel) is 10 gmL^{-1} , Molar mass of Nickel is 60 gmol^{-1} $F = 96500 \text{ C mol}^{-1}$) [4]

- 50) Among H_2 , He_2^+ , Li_2 , Be_2 , B_2 , C_2 , N_2 , O_2^- and F_2 , the number of diamagnetic species is _____ (Atomic numbers: H = 1, He = 2, Li = 3, Be = 4, B = 5, C = 6, N = 7, O = 8, F = 9) [4]

- 51) Let P be the relation defined on the set of all real numbers such that

$$P = (a, b): \sec^2 a - \tan^2 b = 1. \text{ Then P is: [4]}$$

- a) Symmetric and transitive but not reflexive
 b) An equivalence relation
 c) Reflexive and symmetric but not transitive
 d) Reflexive and transitive but not symmetric

- 52) Let ω be a complex number such that $2\omega + 1 = z$

$$\text{where } z = \sqrt{-3}. \text{ If } \begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k, \text{ then } k$$

is equal to [4]

- a) 1
 b) -z
 c) -1
 d) Z

- 53) All the letters of the word PUBLIC are written in all possible orders and these words are written as in a dictionary with serial numbers. Then the serial number of the word PUBLIC is [4]

- a) 578
 b) 580
 c) 576
 d) 582

- 54) The value of $\frac{1}{1!50!} + \frac{1}{3!48!} + \frac{1}{5!46!} + \dots + \frac{1}{49!2!} + \frac{1}{51!1!}$ is:

- [4]
 a) $\frac{2^{51}}{50!}$
 b) $\frac{2^{50}}{50!}$
 c) $\frac{2^{51}}{51!}$
 d) $\frac{2^{50}}{51!}$

- 55) The coefficient of x^{301} in $(1+x)^{500} + x(1+x)^{499} + x^2(1+x)^{498} + \dots + x^{500}$ is: [4]

- a) $^{501}C_{302}$
 b) $^{500}C_{301}$
 c) $^{501}C_{200}$
 d) $^{500}C_{300}$

- 56) Let $\frac{dy}{dx} = \frac{ax-by+a}{bx+cy+a}$, where a, b, c are constants represent a circle passing through the point (2, 5). Then the shortest distance of the point (11, 6) from this circle is: [4]

- a) 7
 b) 10
 c) 5
 d) 8

- 57) Let the function $f(x) = 2x^3 + (2p - 7)x^2 + 3(2p - 9)x - 6$ have a maxima for some value of $x < 0$ and a minima for some value of $x > 0$. Then, the set of all values of p is [4]

- a) $(-\frac{9}{2}, \frac{9}{2})$
 b) $(-\infty, \frac{9}{2})$
 c) $(\frac{9}{2}, \infty)$
 d) $(0, \frac{9}{2})$

- 58) The integral $\int_2^4 \frac{\log x^2}{\log x_2 + \log(36 - 12x + x_2)} dx$ is equal to [4]

- a) 4
 b) 2
 c) 6
 d) 1

- 59) The sides of a rhombus ABCD are parallel to the lines, $x - y + 2 = 0$ and $7x - y + 3 = 0$. If the diagonals of the rhombus intersect at P(1, 2) and the vertex A (different from the origin) is on the y - axis, then the ordinate of A is: [4]

- a) 2
 b) $\frac{5}{2}$
 c) $\frac{7}{4}$
 d) $\frac{7}{2}$

- 60) If the tangent at (1, 7) to the curve $x^2 = y - 6$ touches the circle $x^2 + y^2 + 16x + 12y + c = 0$, then the value of c is [4]

- a) 185
 b) 95
 c) 195
 d) 85

- 61) The equation of a tangent to the parabola, $x^2 = 8y$, which makes an angle θ with the positive direction of X - axis,

is [4]

- a) $X = y \cot \theta + 2 \tan \theta$
 b) $X = y \cot \theta - 2 \tan \theta$
 c) $Y = x \tan \theta - 2 \cot \theta$
 d) $Y = x \tan \theta + 2 \cot \theta$

- 62) If $\frac{dy}{dx} + 2y \tan x = \sin x, 0 < x < \frac{\pi}{4}$ [4]
 a) $\frac{3}{4}$ b) $\frac{1}{8}$
 c) $\frac{1}{4}$ d) $\frac{1}{4}$
- 63) Let $\sqrt{3}\hat{i} + \hat{j}, \hat{i} + \sqrt{3}\hat{j}$ and $\beta\hat{i} + (1 - \beta)\hat{j}$ respectively be the position vectors of the points A, B and C with respect to the origin O. If the distance of C from the bisectors of the acute angle between OA and OB is $\frac{3}{\sqrt{2}}$, then the sum of all possible values of β is [4]
 a) 3 b) 4
 c) 2 d) 1
- 64) The sum of all values of α , for which the points whose position vectors $\hat{i} - 2\hat{j} + 3\hat{k}, 2\hat{i} - 3\hat{j} + 4\hat{k}, (\alpha + 1)\hat{i} + 2\hat{k}$ and $9\hat{i} + (\alpha - 8)\hat{j} + 6\hat{k}$ are coplanar, is equal to [4]
 a) 4 b) 6
 c) - 2 d) 2
- 65) If the mean of the data: 7, 8, 9, 7, 8, 7λ , 8 is 8, then the variance of this data is: [4]
 a) 2 b) 1
 c) $\frac{7}{8}$ d) $\frac{9}{8}$
- 66) Let N denote the number that turns up when a fair die is rolled. If the probability that the system of equations $x + y + z = 1$
 $2x + Ny + 2z = 2$
 $3x + 3y + Nz = 3$ has unique solution is $\frac{k}{6}$ then the sum of value of k and all possible values of N is [4]
 a) 18 b) 20
 c) 21 d) 19
- 67) ABC is a triangular park with $AB = AC = 100$ m. A vertical tower is situated at the mid - point of BC. If the angles of elevation of the top of the tower at A and B are $\cot^{-1}(3\sqrt{2})$ and $\operatorname{cosec}^{-1}(2\sqrt{2})$ respectively, then the height of the tower (in m) is [4]

- a) 25
 b) $10\sqrt{5}$
 c) $\frac{100}{3\sqrt{3}}$
 d) 20

- 68) If $5x + 9 = 0$ is the directrix of the hyperbola $16x^2 - 9y^2 = 144$, then its corresponding focus is [4]
 a) $(\frac{5}{3}, 0)$
 b) $(-\frac{5}{3}, 0)$
 c) (5, 0)
 d) (- 5, 0)
- 69) Let A, B and C be sets such that $\phi \neq A \cap B \subseteq C$. Then which of the following statements is not true? [4]
 a) $B \cap C \neq \phi$
 b) If $(A - C) \subseteq B$, then $A \subseteq B$
 c) $(C \cup A) \cap (C \cup B) = C$
 d) If $(A - B) \subseteq C$, then $A \subseteq C$
- 70) If $S = \{x \in [0, 2\pi] : \begin{vmatrix} 0 & \cos x & -\sin x \\ \sin x & 0 & \cos x \\ \cos x & \sin x & 0 \end{vmatrix} = 0\}$
 then $\sum_{x \in S} \tan(\frac{\pi}{3} + x)$ is equal to [4]
 a) $-2 - \sqrt{3}$ b) $-2 + \sqrt{3}$
 c) $-4 - 2\sqrt{3}$ d) $4 + 2\sqrt{3}$
- 71) If $\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k}$, then the value of $|\hat{i} \times (\vec{a} \times \hat{i})|^2 + |\hat{j} \times (\vec{a} \times \hat{j})|^2 + |\hat{k} \times (\vec{a} \times \hat{k})|^2$ is equal to _____. [4]
- 72) Let α be the area of the larger region bounded by the curve $y^2 = 8x$ and the lines $y = x$ and $x = 2$, which lies in the first quadrant. Then the value of 3α is equal to _____. [4]
- 73) Let $A = \begin{bmatrix} x & 1 \\ 1 & 0 \end{bmatrix}$, $x \in \mathbb{R}$ and $A^4 = [a_{ij}]$. If $a_{11} = 109$, then a_{22} is equal to _____. [4]
- 74) Let a_1, a_2, \dots, a_n be in A.P. If $a_5 = 2a_7$ and $a_{11} = 18$, then $12 \left(\frac{1}{\sqrt{a_{10} + \sqrt{a_{11}}} + \frac{1}{\sqrt{a_{11} + \sqrt{a_{12}}} + \dots + \frac{1}{\sqrt{a_{17} + \sqrt{a_{18}}}} \right)$ is equal to _____. [4]
- 75) The total number of four digit numbers such that each of the first three digits is divisible by the last digit, is equal to _____. [4]